

I B.Tech Supplementary Examinations, Aug/Sep 2008
NUMERICAL METHODS
(Aeronautical Engineering)

Time: 3 hours

Max Marks: 80

Answer any FIVE Questions
All Questions carry equal marks

1. Find the root of the equation $x^3 + x^2 + x + 7 = 0$ correct to three decimal places by.

(a) Bisection method.

(b) Method of false position. [8+8]

2. (a) Given $\sin 45^\circ = 0.7071$, $\sin 50^\circ = 0.7660$, $\sin 55^\circ = 0.8192$ and $\sin 60^\circ = 0.8660$. Find $\sin 52^\circ$ using Newton's interpolation formula. Estimate the error.

(b) Find the second difference of the polynomial $x^4 - 12x^3 + 42x^2 - 30x + 9$ with interval of differencing $h=2$. [12+4]

3. (a) Fit a parabola to the data:

x	1	2	3	4	5	6
y	3	4	7	12	21	32

(b) Find the curve of best fit for the data below:

x	0.5	1	1.5	2	2.5	3
y	1.62	1	0.75	0.62	0.52	0.46

[8+8]

4. (a) Explain Gram-Schmidt orthogonalising process.

(b) Using the Gram-Schmidt orthogonalisation process, compute the first three orthogonal polynomials $P_0(x)$, $P_1(x)$, $P_2(x)$ which are orthogonal on $[0,1]$ with respect to the weight function $W(x)=1$. Using these polynomials, obtain the least squares approximation of second degree for $f(x)=x^{1/2}$ on $[0,1]$. [4+12]

5. (a) Evaluate $\int_0^5 \frac{dx}{4x+5}$ by Simpson's one-third rule and hence find the value of $\log_e 5$ ($n = 10$).

(b) Compute $\int_0^1 \frac{dx}{1+x^2}$ by using Trapezoidal rule, taking $h=0.5$ and $h=0.25$. Compare with exact integration. [8+8]

6. (a) Solve the following equations by Gauss-Jordan method.

$$28x + 4y - z = 32$$

$$x + 3y + 10z = 24$$

$$2x + y + 4z = 35.$$

(b) Solve the following equations by Gauss- elimination method.

$$4x + 2y + z = 14$$

$$x + 5y - z = 10$$

$$x + y + 8z = 20$$

[8+8]

7. (a) Using Euler's method find $y(0.2)$ given $dy/dx = \log(x + y)$ and $y(0) = 1$, $h = 0.2$.

(b) Solve by Taylor series method $dy/dx = y + x^3$ for $x = 1.1, 1.2$ given $y(1) = 1$. [8+8]

8. (a) Solve: $\nabla^2 u = 0$ for the square mesh. As shown in Figure 8a.

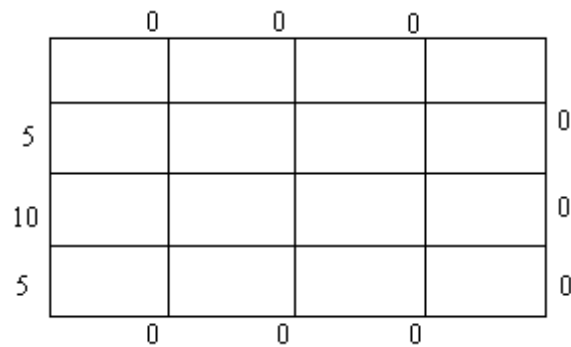


Figure 8a

(b) Derive standard five point formula to solve Laplace equation, stating the assumptions you make. [8+8]

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1. Find the root of the equation $\sin x = e^x - 3x$ correct to three decimal places using

(a) Bisection method.

(b) Method of false position. [8+8]

2. (a) Apply Gauss's forward central difference formula and estimate $f(32)$ from the following table:

x	25	30	35	40
y	0.2707	0.3027	0.3386	0.3794

(b) Find the forward differences of $\frac{1}{(3x+1)(3x+4)(3x+7)}$. [12+4]

3. (a) Fit a straight line to the following data:

x	0.0	0.2	0.4	0.6	0.8	1.0
y	-1.85	-1.20	-0.55	0.15	0.80	1.35

(b) Fit the least square approximation of second degree for the discrete data below:

x	-2	-1	0	1	2
f(x)	15	1	1	3	19

[8+8]

4. (a) Show that $\sum_{i=-\infty}^{\infty} B_i^k$ is a constant function.

(b) Show that the Fourier transform of $e^{-x^2/2}$ is $e^{-s^2/2}$ [8+8]

5. (a) Dividing the range into 10 equal parts, find the approximate value of $\int_0^{\pi} \sin x \, dx$ by

i. Trapezoidal rule

ii. Weddle's rule.

(b) Compute $\int_0^{\pi} \sin x \, dx$ by using Simpson's rule with 12 subdivisions. [8+8]

6. (a) Show that the system

$$2x - 3y + z = 0$$

$$4x + 9y + z = 0$$

$$8x - 27y + z = 0$$

has no non-trivial solution.

- (b) Apply Gauss Elimination and solve the system.

$$2x+3y+4z=9$$

$$3x+y+2z=6$$

$$x+y+3z=5.$$

[8+8]

7. (a) Using Euler's method find $y(0.2)$ given $dy/dx = \log(x+y)$ and $y(0) = 1$, $h = 0.2$.
- (b) Solve by Taylor series method $dy/dx = y + x^3$ for $x = 1.1, 1.2$ given $y(1) = 1$. [8+8]
8. (a) Derive the explicit finite difference scheme for solving the one dimensional hyperbolic equation $u_{tt} - a^2 u_{xx} = 0$, $0 < x < l$, $t > 0$ subject to $u(0,t)=u(l,t)=0$, $u(x,0)=h(x)$ and $\frac{\partial u}{\partial t}(x,0)=g(x)$, $0 \leq x \leq l$.
- (b) The function u satisfies Laplace's equation at all points within the square given in the following Figure 8b and has the boundary values indicated. Compute a solution correct to two decimals by Gauss-seidel method. [8+8]

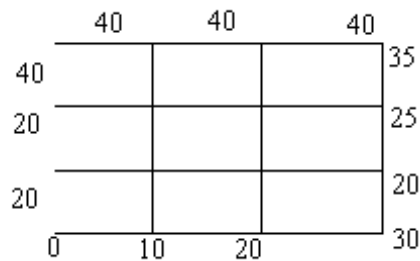


Figure 8b

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1. Find the root of the equation $\sin x = 1 + x^3$ between $(-2, -1)$ using

(a) Regular falsi method.

(b) Newton's method.

[8+8]

2. Find the value of $y(21)$ and $y(28)$ from

x	20	23	26	29	32
y	0.3420	0.3907	0.4384	0.4848	0.4951

[16]

3. (a) Fit a curve of the form $y = ax^b$ to the data:

x	1	2	3	4	5	6
y	1200	900	600	200	110	50

(b) Fit a parabola $y = a + bx + cx^2$ to the following data:

x	2	4	6	8	10
y	3.07	12.85	31.47	57.38	91.29

[8+8]

4. Show that on $[t_i, t_{i+1}]$ we have $B_i^k(x) = \frac{(x-t_i)^k}{(t_{i+1}-t_i)(t_{i+2}-t_i)\dots(t_{i+k}-t_i)}$ [16]

5. (a) From the following table of values of x and y , $\frac{dy}{dx}$ at each of the points by fitting the Cubic Spline method.

x	1	2	3	4
y	1	3	4	2

(b) Using Simpson's $3/8^{\text{th}}$ rule evaluate $\int_0^6 \frac{dx}{1+x^2}$ by dividing the range into 6 equal parts. [8+8]

6. (a) Solve by Gauss elimination method.

$$10x + 2y + z = 9$$

$$2x + 20y - 2z = -44$$

$$-2x + 3y + 10z = 22.$$

(b) Using Gauss-Jordan method solve.

$$2x - 3y + 4z = 7$$

$$5x - 2y + 2z = 7$$

$$6x - 3y + 10z = 23.$$

[8+8]

7. (a) Using Euler's method find $y(0.2)$ given $dy/dx = \log(x + y)$ and $y(0) = 1$, $h = 0.2$.
- (b) Solve by Taylor series method $dy/dx = y + x^3$ for $x = 1.1, 1.2$ given $y(1) = 1$. [8+8]
8. (a) Solve
 $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$, subject to (a) $u(0, y) = 0$, for $0 \leq y \leq 4$
 (b) $u(4, y) = 12 + y$, for $0 \leq y \leq 4$ (c) $u(x, 0) = 3x$, for $0 \leq x \leq 4$
 (d) $u(x, 4) = x^2$, for $0 \leq x \leq 4$
 dividing the square into 16 square meshes of side 1.
- (b) Solve $\nabla^2 u = 0$ (the two dimensional heat conduction equation in steady-state) at the interior lattice points, given boundary values as follows solve by Jacobi's method. As shown in Figure 8b. [8+8]

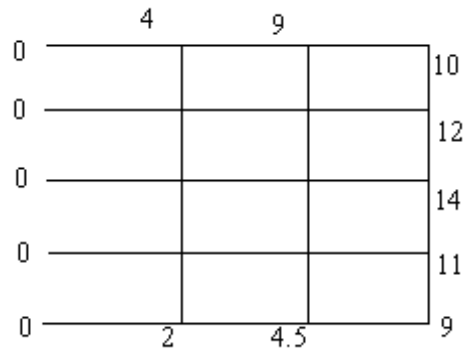


Figure 8b

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1. Find the root of the equation $x^3 - x - 11 = 0$ correct to four decimals using.
- (a) bisection method
 (b) Method of False position. [8+8]

2. The probability integral $P = \sqrt{\frac{2}{\pi}} \int_0^x \exp(-\frac{1}{2}t^2) dt$ has the following values :

x	1.00	1.05	1.10	1.15	1.20	1.25
y	0.682689	0.706282	0.728668	0.749856	0.769861	0.788700

Calculate P for $x=1.025$ and $x=1.235$. [16]

3. (a) Fit a straight line $y=a+bx$ to the data:

x	1	2	3	4	5	6
y	2.4	3.1	3.5	4.2	5.0	6.0

- (b) Derive the condition for linear weighted least squares approximation. [8+8]

4. (a) Prove that the orthogonal polynomials satisfy a three-term recurrence relation.
 (b) Find the Fourier transform of $e^{-a|x|}$ if $a > 0$. Deduce that $\int_0^{\infty} \frac{1}{(x^2+a^2)^2} dx = \frac{\pi}{4a^3}$ if $a > 0$. [8+8]

5. (a) Dividing the range into 10 equal parts, find the approximate value of $\int_0^{\pi} \sin x dx$ by

- i. Trapezoidal rule
 ii. Weddle's rule.

- (b) Compute $\int_0^{\pi} \sin x dx$ by using Simpson's rule with 12 subdivisions. [8+8]

6. (a) Show that the system $x+2y+3z=6; x+3y+5z=9; 2x+5y+9z=6$ has no non-trivial solution.

- (b) Using Gauss-Jordan method solve $\begin{bmatrix} 1 & 2 & 1 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 8 \\ 13 \\ 5 \end{bmatrix}$ [8+8]

7. (a) Using Euler's method find $y(0.2)$ given $dy/dx = \log(x+y)$ and $y(0) = 1, h = 0.2$.

- (b) Solve by Taylor series method $dy/dx = y + x^3$ for $x = 1.1, 1.2$ given $y(1) = 1$. [8+8]
8. (a) Solve: $\nabla^2 u = 0$ in the square region bounded by $x = 0, x = 2, y = 0, y = 2$ and with boundary conditions $U(x,0) = (x^2/2) = 0, U(x,2) = x^2$ by taking $h=k=0.5$ and with boundary conditions $u(0, y) = 0, u(2, y) = 8 + 2y$.
- (b) Solve the equation $u_{xx} + u_{yy} = 0$ in the domain of following Figure 8b by Gauss seidel method. [8+8]

	0.5	0.5	
	u ₁		u ₂
0			0
0	u ₃		0
	0	0	

Figure 8b
